

See discussions, stats, and author profiles for this publication at: <https://www.researchgate.net/publication/220796058>

# A Fuzzy-Graph-Based Approach to the Determination of Interestingness of Association Rules

Conference Paper in Lecture Notes in Computer Science · December 2002

DOI: 10.1007/3-540-36277-0\_34 · Source: DBLP

CITATION

1

READS

28

2 authors:



**B. Shekar**

Indian Institute of Management Bangalore

31 PUBLICATIONS 168 CITATIONS

[SEE PROFILE](#)



**Rajesh Natarajan**

University Carlos III de Madrid

18 PUBLICATIONS 92 CITATIONS

[SEE PROFILE](#)

Some of the authors of this publication are also working on these related projects:



Interestingness of Association rules [View project](#)

# A Fuzzy-Graph-Based approach to the determination of Interestingness of Association Rules

B. Shekar and Rajesh Natarajan  
*Indian Institute of Management Bangalore,  
Bangalore, India*

# Knowledge Management

- ✍ Knowledge- a significant organizational resource
- ✍ Knowledge Management Systems (KMS)
- ✍ Knowledge creation, storage/retrieval, transfer and application
- ✍ Tacit knowledge

# Knowledge Discovery in Databases

Knowledge discovery in databases (KDD) is the non-trivial process of identifying **valid, novel, potentially useful** and **ultimately understandable patterns** in large databases (*Fayyad, et al., 1996*)

# Association Rules

- ✍ Implication rules that bring out hidden relationships among attributes and/or items using **co-occurrence** as the basis.
- ✍ Bring out natural **affinity** between items purchased together in customer transactions
- ✍ Cannot indicate the exact nature of relationship
- ✍ Useful in exploratory studies

# Association Rules (Cont'd.)

An Association Rule is defined to be an implication rule of the form

$$A \Rightarrow B,$$

where  $A, B \subseteq I$  and  $A \cap B = \emptyset$

i.e.  $A$  and  $B$  can be a single item or a set of items from  $I$  and there is no item that is common to the sets  $A$  and  $B$ .

# Association Rules (Cont'd.)

Rule : A ? B

**Support ?  $\frac{\text{No. of transactions containing A and B}}{\text{Total no. of transactions in the database}}$**

**Confidence ?  $\frac{\text{No. of transactions containing A and B}}{\text{Total no. of transactions containing A}}$**

# Association Rules (Cont'd.)

## *Bread ? Butter*

{conf.= 80% support=10%} means

"that 80% of the transactions that *contain bread also tend to contain butter*, and they together occur in 10% of the overall transactions"





# Characteristics of Association Rule Mining Algorithms

- ✍ Massive search through the database
- ✍ Complete examination of the database
- ✍ Parameters of the rules are exact, no estimation
- ✍ Very High Demands on I/O, Memory and Computation
- ✍ High Degree of Automation: Very little user interaction

# Consequences

## Large number of Rules Discovered (**Rule Quantity problem**)

-  Example: Census database, No. of rules generated=23,712 (*Brin, Motwani, et al., 1997*)
-  Telephone company fault management (Simultaneous faults occurrence in a network)  
Rules generated=1,426 (*Mannila, et al., 1994*)

## Many of the rules are obvious to the user/domain expert (**Rule Quality problem**)

- e.g. Has Licence ? Age >18;  
"five year olds do not work"  
"Unemployed residents do not earn income from work"  
(*Brin, Motwani, et al., 1997*)

# Consequences

- ✍ Really novel, relevant, useful and interesting rules are very few
  - ✍ **Example:** Rules from a Hurricane Database (*Major and Mangano, 1995*)
  - ✍ Started with 529 rules and ended up with only 19 rules that were really useful and relevant.
- ✍ Very difficult for the domain expert/user to get an overview of the domain
- ✍ Typical users have limited time at their disposal

# Interestingness Measures

- ✍️ Quantify the amount of interest that a rule(pattern) is supposed to evoke in a user examining it
- ✍️ Elusive concept that is very difficult to capture (*Silberschatz, 1996*)
- ✍️ Objective and Subjective
- ✍️ Actionability, Unexpectedness, User Knowledge/Goals, Anticipation

# Item Relatedness

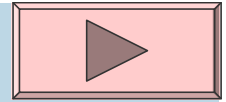
- ✍ Relationships between items
  - ✍ Generic categories (primary functional purpose)
  - ✍ Secondary functionalities
  - ✍ Domains of application
- ✍ Item-pairs in Association Rules have high frequency of occurrence
- ✍ Item pairs that contain unrelated or weakly related items are interesting
- ✍ *Bread ? Butter*
- ✍ *Chocolate ? Paper Napkins, Chocolate ? Pencils*
- ✍ *Beer? Diapers*

# Approach towards Finding Interestingness of Association rules

- ✍ Relationships between items are captured in the structure of a Fuzzy Taxonomy
- ✍ Define an Item-relatedness measure based on the structural aspects of the Fuzzy Taxonomy
- ✍ Find out the relatedness between item-pairs
- ✍ Combine relatedness to arrive at an interestingness value for the rule

# Fuzzy Taxonomy

- ✍ Extension of the traditional concept hierarchy (taxonomy) tree
- ✍ Allows us to express the following kinds of relationships
  - ✍ An item belonging to two or more higher-level concepts
  - ✍ Items used to substitute the functions of other items to various extents (e.g. spoon, knife etc.)



# Fuzzy Taxonomy

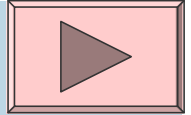
- ✍ A child need not be a full member of the category/concept of parent
- ✍ Connections restricted between leaf-level items and higher-level concept nodes
- ✍ Membership function: Extent to which the child node belongs to its parent ;  $\mu ? [0,1]$
- ✍ Membership Transfer: Child to parent to ancestors
- ✍ Membership Transfer: Membership grade of a child node 'c' in its ancestor 'a'

$$\mu_{(c,a)} = \max\{ \mu_{(c,a)}(k) \}$$

where  $k = 1, 2, \dots, N$ .

$\mu_{(c,a)}(k)$  is the membership grade of the child node 'c' in its ancestor 'a' by the virtue of the path 'k'.





# Highest-level node of path

$[H_{A, B} (p)]$

- ✍ Node that occurs at the highest level (i.e. nearest to the root node) in the simple path 'p' connecting items A and B
- ✍ Plays a pivotal role in determining relatedness between items
- ✍ Closest common context that relates the two items



# Highest-level Node Membership $[HM_{A, B}(p)]$

$$HM_{A, B}(p) = \min [ \mu_{A, H(A, B)}(p), \mu_{B, H(A, B)}(p) ]$$

example:  $HM_{(knife, shoes)}(p) = \min [0.5, 0.6] = 0.5$ ;  
where the path 'p' is the fuzzy path connecting  
the two items

**Why minimum?**

# Highest-level Relatedness



## $[HR_{A,B}(p)]$

- ✍ Two siblings at higher level of a taxonomy are less related to each other as compared to two siblings at a lower level of the taxonomy
- ✍ Longer path from root node to highest-level node implies higher relatedness (Why?)
- ✍  $HR_{A,B}(p) = \text{level}[H_{A,B}(p)]$

# Node Separation Relatedness

## [ $NSR_{A,B}(p)$ ]

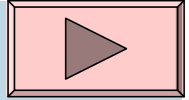


- ✍ Length of path connecting two items indicates the conceptual distance between them.
- ✍  $NSR_{A,B}(p)$  = Length of the simple path 'p' connecting nodes A and B
- ✍ Inversely related to 'relatedness'

# Overall Relatedness

- ✍ Each path between two items contributes a component of relatedness between the two items

$$\mathbf{OR}_{A,B}(\mathbf{p}) = \frac{(\mathbf{1} - \mathbf{HR}_{A,B}(\mathbf{p}))(\mathbf{HM}_{A,B}(\mathbf{p}))}{\mathbf{NSR}_{A,B}(\mathbf{p})}$$

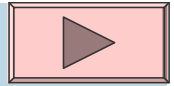


# Total Relatedness

$$TR(A,B) = \sum_p \frac{OR_{A,B}(p)}{K} \sum_p \frac{(1 - HR_{A,B}(p))(HM_{A,B}(p))}{K - NSR_{A,B}(p)}$$

Total Relatedness varies from 0 to p,  
where 'p' is the maximum number of paths that  
exist between two items

# Determination of total relatedness between *Knife and Shoes* (Table 1)



Path	A= Knife	B= Shoes	NSR	HR	HM	OR
I	Crisp (1.0)	Crisp (1.0)	3	1	1.0	0.166
II	Fuzzy (0.5)	Fuzzy (0.6)	5	1	0.5	0.05
III	Fuzzy (0.5)	Crisp (1.0)	6	0	0.5	0.021
IV	Crisp (1.0)	Fuzzy (0.6)	6	0	0.6	0.025



**Table 2: A comparison of Item Relatedness for sample item-pairs.**

No	Item A	Item B	Path I (Crisp Crisp)	Path II (Fuzzy Fuzzy)	Path III (Fuzzy Crisp)	Path IV (Crisp Fuzzy)	TR (A, B)
1	Knife	Shoes	0.1668	0.05	0.020825	0.025	0.2626
2	Shoes	Safety Shoes	0.0417	0.0167	0.6	0.3	0.9583
3	Spoon	Shoes	0.1667	----	----	0.025	0.19175
4	Spoon	Safety Shoes	0.0417	----	----	0.0667	0.10835
5	Knife	Industri- al Knife	0.0417	0.0125	0.5	0.225	0.77918



# Advantages


- ✍ Gradual development of the Fuzzy Taxonomy by an iterative process
- ✍ Easier for a manager to give his views
- ✍ Tacit knowledge of managers is brought out
- ✍ Only rules as identified as interesting need to be examined

# Applications

 Shelf-space design

 Display design

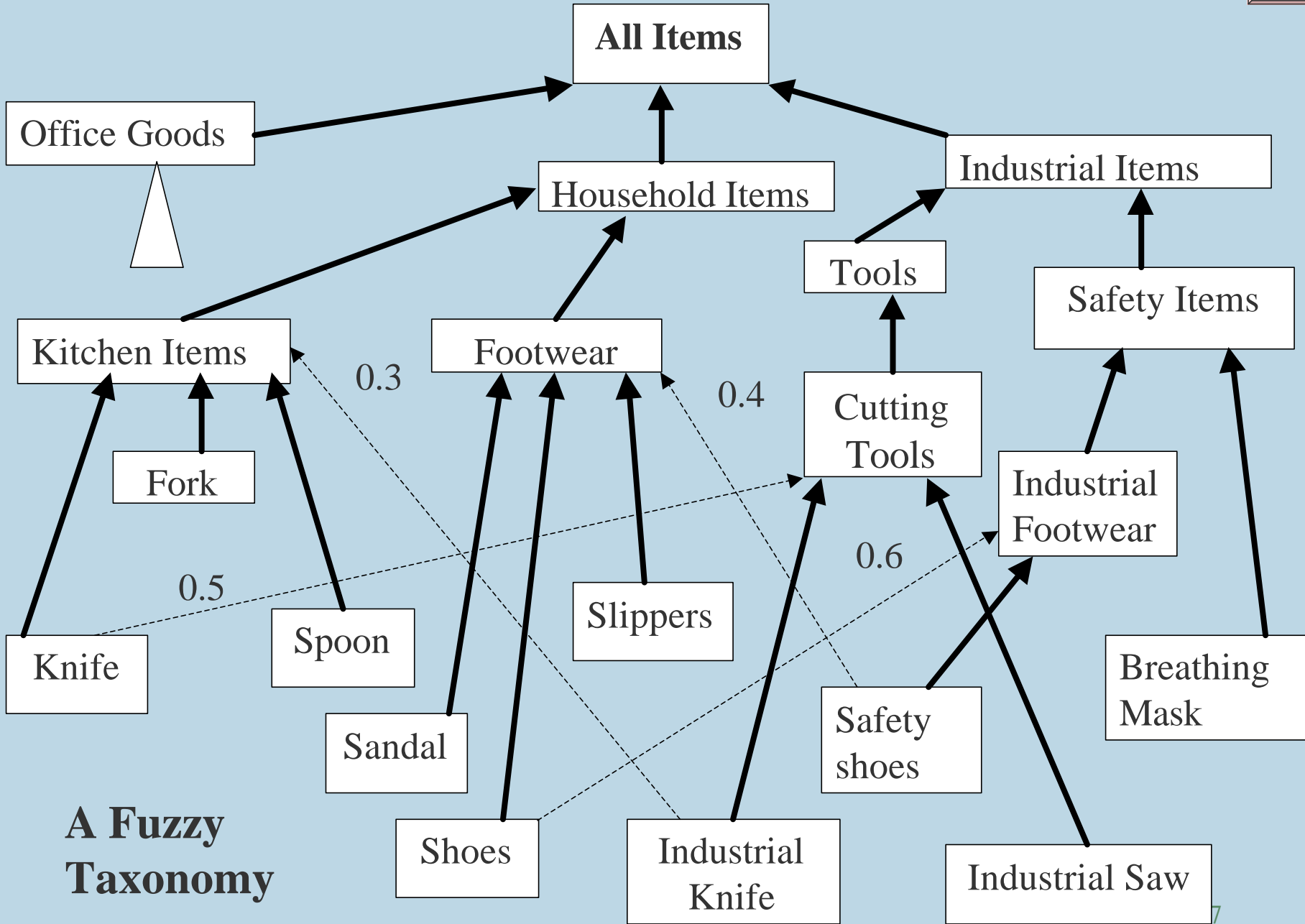
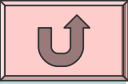
 Discount coupons design

 Selection of products for  
product bundling to induce  
sales



# Thank You

Questions, Clarifications,  
Comments, Suggestions,..... are  
**Most Welcome**



## A Fuzzy Taxonomy

# Algorithm

Compute all paths between an item and root node

$Path[A,B,k]=$

$\{[Ipath(A,i)? Ipath(B,j)]-[Ipath(A,i)? Ipath(B,j)]\}$   
 $? H[Ipath(A,i)? Ipath(B,j) ]$

where

$Ipath(A,i)$  = ith path between A and root node

$Ipath(B,j)$  = jth path between B and root node

$H [Ipath(A,i)? Ipath(B,j) ]$  = highest-level node

# Use of Relatedness to Compute Interestingness of ARs

✍ Interestingness and Relatedness are opposing notions

✍ Relatedness: Item Pairs

✍ AR:  $A \rightarrow B$

✍ Antecedent Item Pairs


✍  $(\{a_i, a_j\}, \text{ where } i \neq j \text{ and } a_i \rightarrow A)$

✍ Consequent Item Pairs

✍ a pair  $\{b_i, b_j\}$  where  $i \neq j$  and  $b_i \rightarrow B$

# Use of Relatedness to Compute Interestingness of ARs (Cont'd)

## Antecedent-Consequent Item Pairs

 a pair  $\{a_i, b_j\}$  where  $a_i \rightarrow A$  and  $b_j \rightarrow B$ ,  
 $A \rightarrow B = I$  and  $A, B \rightarrow I$ .

 Different Item-pairs might have different Interestingness for Users

 Relatedness Values for all such pairs are computed

# Interestingness Measure

$$I = \frac{m_1}{m_1 + m_2 + m_3} \cdot \frac{1}{\min TR(AP)} + \frac{m_2}{m_1 + m_2 + m_3} \cdot \frac{1}{\min TR(CP)} + \frac{m_3}{m_1 + m_2 + m_3} \cdot \frac{1}{\min TR(ACP)}$$

$\min TR(AP) = \text{minimum} (TR(a_i, a_j)) \cdot \{a_i, a_j\} / a_i$  A and  $i \neq j$  ;

$\min TR(CP) = \text{minimum} (TR(b_i, b_j)) \cdot \{b_i, b_j\} / b_i$  B and  $i \neq j$  ;

$\min TR(ACP) = \text{minimum} (TR(a_i, b_j)) \cdot \{a_i, b_j\} / a_i$  A and  $b_j \in B, A \cap B = \emptyset$  and  $A, B \subseteq I$ ;



# Interestingness Measure

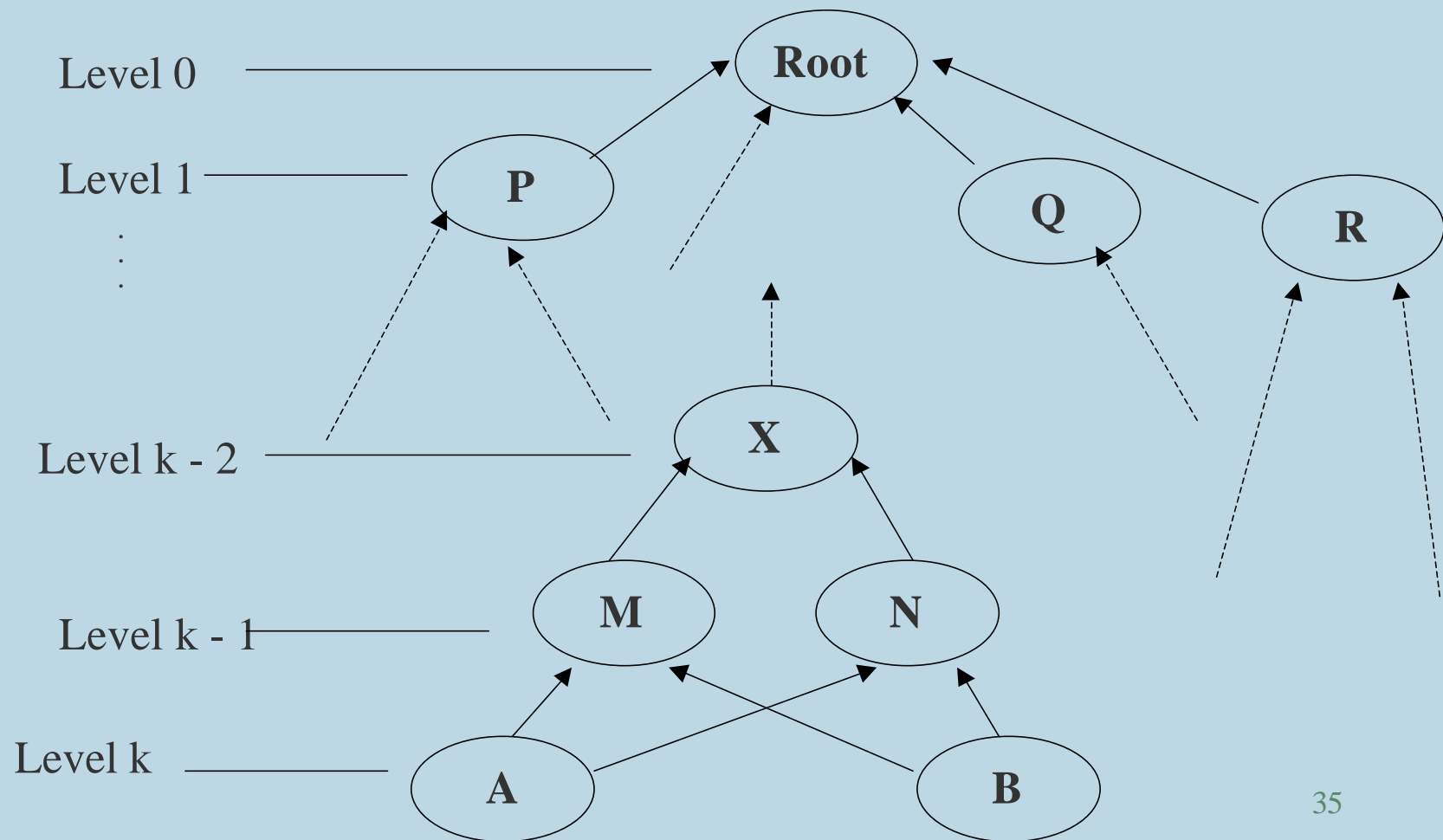
- ✍  $m_1$ ,  $m_2$  and  $m_3$  are three numbers used to appropriately weigh the interestingness of antecedent, consequent and antecedent-consequent pairs respectively
- ✍ Here,  $m_1 = m_2 = m_3 = 1$
- ✍ Implicit assumption: Greater number of conditions gives more information; leads to greater interestingness
- ✍ Direction of rule not consequential

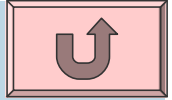
Sr. No.	(Table 3) Rule	I $m_1, m_2, m_3=1$
1	{Knife}? {Shoes}	1.2693
2	{Spoon} ? {Shoes}	1.7384
3	{Industrial Knife} ? {Safety Shoes}	1.8601
4	{Knife}? {Safety Shoes}	1.9043
5	{Knife} ? {Shoes, Safety Shoes}	1.9391
6	{Industrial Knife} ? {Shoes}	2.0305
7	{Knife, Industrial Knife} ? {Safety Shoes}	2.3321
8	{Industrial Knife} ? {Shoes, Safety Shoes}	2.3783
9	{Knife, Industrial Knife} ? {Shoes}	2.4583
10	{Knife, Industrial Knife} ? {Shoes, Safety Shoes}	2.8061
11	{Spoon} ? {Safety Shoes}	3.0764

# Related Work

- ✍ Taxonomies: Generalized ARs (Srikant et al., 1995), Negative ARs (Navathe, et al., 1998)
- ✍ Fuzzy Taxonomy (Chen et al. 2000)
- ✍ Interestingness in Fuzzy Taxonomies (Graff et al., 2000, 2001)
- ✍ Interestingness of Summaries (Hamilton et al., 1995)
- ✍ Text Mining (Basu, et al., 2001)
- ✍ Noun Sense Disambiguation (Lin et al., 2002)

# Maximum Relatedness Contributed by a path





# Maximum Relatedness Contributed by a path

- ✍ Maximum relatedness contributed by a path in a fuzzy taxonomy of depth  $k$  is ' $k$ '
- ✍ Use ' $k$ ' to normalize the measure
- ✍ Each contribution varies from 0 to 1

# Approaches in Literature

- ✍ Rule Templates (*Klemettinen et al., 1994*)
- ✍ Rule Covers (*Toivonen, 1995*)
- ✍ Mining specific kinds of association patterns  
(Negative Association rules, Profile Association rules, Cyclic rules etc.)
- ✍ Summarization (GSE patterns)
- ✍ Grouping and Clustering
- ✍ Interestingness Measures

# Rule Templates

- ✍ General structure of the rule given by the user in the form of inclusive/restrictive templates
- ✍ Neural Networks ? Design and Analysis of Algorithms (0.48, 0.02)
- ✍ Template: Graduate Course, Any Course ? Design and Analysis of Algorithms
- ✍ User explicitly gives what is interesting and what is not.

# General Rules, Summaries and Exceptions (Liu, Hu et al. 2000)

## Example of a GSE pattern

(General Rule, summary and Exceptions)

$A1=a \Rightarrow X$  (sup=41%, conf=77%)

Except R7:  $A1=a, A2=b \Rightarrow Y$

(sup=10%, conf=83%)



# Objective Measures of Interestingness

- ✍ Depend on the structure of the pattern
- ✍ Underlying data used in the discovery process
- ✍ Domain Independent
- ✍ Each measure looks at a specific aspect of the data
- ✍ Cannot capture all the complexities of the pattern discovery process

# Objective Measures of Interestingness: Examples

- ✍ Discovery of Surprising patterns like Simpson's Paradox
- ✍ Statistical Measures like: support, confidence, conviction, implication, rule interest etc.
- ✍ Information theoretic measures like Entropy, Gini, J-Measure, Hellinger Measures etc.

# Subjective Measures of Interestingness

- ✍ Also depend on the **User** who examines the pattern in addition to structure of the pattern and the characteristics of the data/data generating process
- ✍ Mostly Domain Dependent
- ✍ Unexpectedness (*Silberschatz, 1996*)
- ✍ Actionability (Usefulness) (*Adomavicius, et al. 1997*)
- ✍ Anticipation (*Roddick and Rice, 2001*)
- ✍ User Goals/User Knowledge (*Ram, A. ; 1990*) <sup>42</sup>

# Subjective Measures of Interestingness

## *General Approach*

1. Elicit user opinions/beliefs
2. Express them in a form suitable for computation/Measure for comparison
3. Mine patterns from the database
4. Compare User Opinions with mined patterns
5. Patterns that deviate the most from user beliefs are deemed interesting

